If $x$ and $y$ are real numbers such that $x + y = c = \text{const}$, prove that $xy$ achieves its maximum if and only if $x = y$. 