

Credit Card Acceptance and Product Quality

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MOTIVATION

- Credit card network merchant discount fees run from 1% to 3%.
- Credit card issuers act as a buyer's attorney in the case of defective merchandise.
- Credit card acceptance indicates product quality.

Paying in full with a credit card gives useful protection against faulty goods costing between £100 and £30,000. If you have a complaint about a purchase you have made with your NatWest Credit Card, please contact the retailer first. If the retailer can't resolve the issue or has gone out of business, contact us and we will take up the matter on your behalf.

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- Firms face moral hazard problem: product quality unobserved until sale occurs

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- Mass 1 of buyers, mass \bar{n} of sellers (in the DM)
- Infinite lives

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- High effort costs a seller k , low effort costs 0.

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- Common discount factor, $\beta < 1$ between periods
- Lifetime utility of an individual type $i = b, s$ is $\sum_{t=0}^{\infty} \beta^t U_t^i$.

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- (Produced goods that do not sell rot at the end of the period.)

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- Last assumption requires $\rho \geq 1$.

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Where

$$W(\pi, x) = (x - c(x))(1 + \bar{n}) + \alpha(\bar{n}) [\pi \lambda_h + (1 - \pi) \lambda_l] u - \bar{n} \pi k.$$

and π is the share of sellers of the DM good who exert effort.

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- Implementation is through contingent transfers

- Some medium of exchange is essential for trade in the DM.
- Buyers can use money or a credit card to purchase goods.
- Money is perfectly divisible and agents can hold any non-negative amount.
- Aggregate nominal money supply, M_t , grows at constant gross rate $\gamma < \beta$ so that $M_{t+1} = \gamma M_t$.
- New money is injected (or withdrawn if $\gamma < 1$) by lump-sum transfers (taxes) in the CM.
- Transfers go only to buyers
- Price of CM goods is normalized to 1 the relative price of money is denoted ϕ_t .
- Let $z_t = \phi_t m_t$ be the real value of an amount of money m_t .

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Definition

A symmetric equilibrium is a set of active submarkets, $\Gamma \subset R_+^2$, to the DM, a function, $\Lambda(z, \theta)$, that specifies the proportion of high quality goods in submarket (z, θ) , a function, $n(z, \theta)$, that specifies how many sellers enter submarket (z, θ) , and a propensity, π^* , for sellers to exert high effort such that:

- 1 Given $\Lambda(., .)$ every $(z^*, \theta^*) \in \Gamma$ solves the buyers' problem for $(\hat{z}, \hat{\theta})$.
- 2 Every $(z^*, \theta^*) \in \Gamma$ solves the sellers' problem for $(\hat{z}_i, \hat{\theta}_i)$ for $i = h$ or l .
- 3 Rational expectations holds:

$$\pi^* = \int_{\Gamma} \left(\frac{\Lambda(z, \theta) - \lambda_l}{\lambda_h - \lambda_l} \right) \frac{n(z, \theta)}{\bar{n}} dz d\theta.$$

- 4 The population constraints for sellers and buyers hold:

$$\int_{\Gamma} n(z, \theta) dz d\theta = \bar{n}, \quad \int_{\Gamma} \frac{n(z, \theta)}{\theta} dz d\theta = 1.$$

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- There exists a unique equilibrium (z^*, θ^*) so that $\theta^* = \bar{n}$.

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- Prices become common knowledge and are used by buyers to direct their search.

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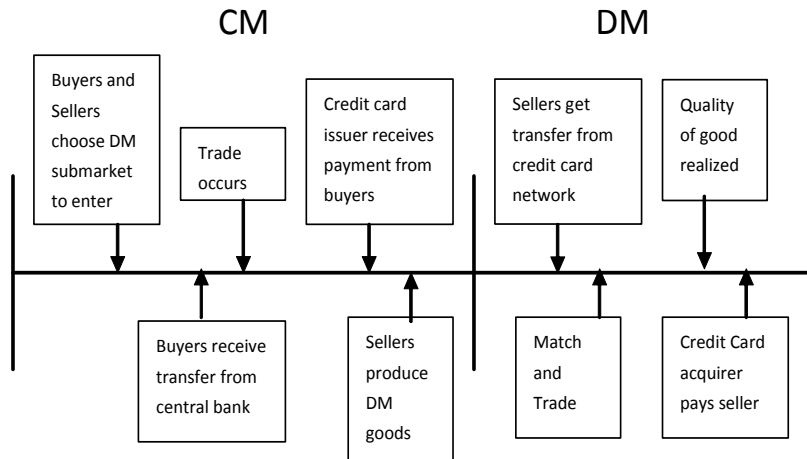
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- There is a credit card company that sets ω and runs the network at zero cost.
- Any profits are disbursed to sellers at the beginning of the DM

TIMELINE



CREDIT/CASH ECONOMY

- Seller separated equilibria sought
- Submarkets of the DM are indexed by (p, z, θ, ψ, i) ,
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Definition

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- 1 Separation of sellers: $(p, z, \theta, \psi, h) \in \Omega \Rightarrow (p, z, \theta, \psi, l) \notin \Omega$
- 2 Individual rationality: every $(p, z, \theta, \psi, i) \in \Omega$ solves the buyers' and sellers' problems
- 3 Buyer population constraint: $1 = \int_{\Omega} \frac{n(p, z, \theta, \psi, i)}{\theta} dp dz d\theta d\psi di$
- 4 Seller population constraint: $\bar{n} = \int_{\Omega} n(p, z, \theta, \psi, i) dp dz d\theta d\psi di$
- 5 RE: $\tilde{\pi}^* = \frac{1}{\bar{n}} \int_{\Omega} n(p, z, \theta, \psi, h) dp dz d\theta d\psi,$
 $\tilde{\psi}^* = \int_{\Omega} \psi \theta n(p, z, \theta, \psi, i) dp dz d\theta d\psi di.$

- Buyer indifference:

$$\alpha(\theta_i)\lambda_i p_i = z_i \left[\frac{\gamma}{\beta} - 1 + \alpha(\theta_i) \right] \quad i = h, l.$$

where θ_i , p_i , z_i are the equilibrium values associated with effort level $i = h, l$.

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- Sellers indifference

$$\lambda_i(1 - \omega)p_i = z_i \quad i = h, l.$$

- Buyer indifference:

$$\alpha(\theta_i)\lambda_i p_i = z_i \left[\frac{\gamma}{\beta} - 1 + \alpha(\theta_i) \right] \quad i = h, l.$$

where θ_i , p_i , z_i are the equilibrium values associated with effort level $i = h, l$.

- Sellers indifference

$$\lambda_i(1 - \omega)p_i = z_i \quad i = h, l.$$

- If $\omega = 0$ and $\gamma = \beta$ they coincide.

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- This also means that as long as $z_i > \lambda_i(1 - \omega)p_i$ the cash price offered is moot.

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- If a buyer has a 50% chance of making the purchase then $\omega(\gamma, \bar{n}) \approx 0.24\%$.

HIGH EFFORT CREDIT ONLY EQUILIBRIUM

- In a high effort credit only equilibrium (when it exists):

$$\begin{aligned}\theta_h &= \bar{n} & p_h &= \frac{u\eta(\bar{n})\gamma}{\beta} \\ z_h &> \lambda_h(1 - \omega(\gamma, \bar{n}))p_h\end{aligned}$$

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INCENTIVE CONSTRAINT 1

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- Offering a viable cash price tells buyers that the seller has not incurred high effort.
- Any attempt to offer $z_h < \lambda_h(1 - \omega(\gamma, \bar{n}))p_h$ would open a new market.

INCENTIVE CONSTRAINT 2

Sellers will not choose low effort and enter the high effort market.

- $$\left(\frac{\alpha(\bar{n})\beta p_h(1-\omega)}{\bar{n}\gamma} \right) \lambda_h - k \geq \left(\frac{\alpha(\bar{n})\beta p_h(1-\omega)}{\bar{n}\gamma} \right) \lambda_l$$

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- $\eta(\cdot) < 1$ means even with $\omega = 0$, market economy cannot always achieve first-best.

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 - No simple algebraic expression emerges

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- Maximal value of $\omega_{\max} = 4.37\%$.