Financial Economics	Arbitrage and Option Pricing	Financial Economics	Arbitrage and Option Pricing	
Arbitrage				
<i>Arbitrage</i> refers to the simultaneous purchase and sale in different markets to achieve a certain profit.		<b>Option Pricing</b> Based on the principle that no arbitrage opportunity can exist, one can develop an elaborate theory of option pricing.		
In market equilibrium, there must be no opportunity for profitable arbitrage.				
Otherwise one could make a certain profit by buying low (buying the undervalued asset) and selling high (selling the overvalued asset). There would be excess demand for the former and excess supply for the latter.				
1		2		
Financial Economics	Arbitrage and Option Pricing	Financial Economics	Arbitrage and Option Pricing	
<b>Option-Price Table</b>				
Call option prices for Tandy stock:				
April July	v October			
$40  3\frac{5}{8}  5\frac{5}{8}$	1	Pat	tterns	
$45  \frac{15}{16}  2\frac{5}{8}$	$4\frac{5}{8}$	What pricing patterns are present in the table?		
$50 \frac{5}{16}$	$2\frac{1}{2}$			
The table shows nine option prices, for three striking prices and three expiration dates. The spot price is $42\frac{7}{8}$ . Hence the 40 calls are in-the-money, and				
				the 45 and 50 calls are out-of-the-money.
3				
Financial Economics	Arbitrage and Option Pricing	Financial Economics	Arbitrage and Option Pricing	
		Example		
<b>Expiration Date</b>		Suppose that the 40-July option price was 8.		
The price rises as the expiration date becomes more distant.		Since one makes an arbitrage profit by buying low and selling high, one buys the undervalued option and sells the overvalued option.		
This property conforms with the general principle that expanding one's possible choices has value.				
However one can say more: if the price were less for a more distant expiration date, then one could make an arbitrage profit.		Hence buy a 40-October option and sell a 40-July option.		
		One makes an immediate gain of $1 = 8 - 7$ . Then what do you do?		
5			6	

Financial Economics	Arbitrage and Option Pricing	Financial Economics	Arbitrage and Option Pricing	
<b>Option is Exercised</b> If the 40-July option is exercised, you immediately exercise the 40-October option. These two transactions cancel, and your overall profit is 1.		<b>Option is Not Exercised</b> Alternatively, the 40-July option might never be exercised. You still have the 40-October option, and perhaps you can exercise it for additional profit. Your overall profit is therefore at least 1, and perhaps more.		
7		8		
Financial Economics	Arbitrage and Option Pricing	Financial Economics	Arbitrage and Option Pricing	
<section-header><section-header><text><text><text></text></text></text></section-header></section-header>		Example Suppose that the 45-October option price was 8. Since one makes an arbitrage profit by buying low and selling high, one buys the undervalued option and sells the overvalued option. Hence buy a 40-October option and sell a 45-October option. One makes an immediate gain of 1 = 8 - 7. Then what do you do?		
Financial Economics Option	Arbitrage and Option Pricing is Exercised	Financial Economics Option is	Arbitrage and Option Pricing Not Exercised	
If the 45-October option is exercised, you immediately exercise the 40-October option. You are buying a share for 40 and selling a share for 45, so you make a profit of 5. Your total profit is therefore 6.		Alternatively, the 45-Octobe You still may be able to exer profit. Your overall profit is t more.	r option might never be exercised. cise the 40-October option at a therefore at least 1, and perhaps	

Financial Economics	Arbitrage and Option Pricing	Financial Economics	Arbitrage and Option Pricing
No Exercise			
It does not pay to exercise an option prior to the expiration date.			
Although one could profit by exercising an in-the-money option, one would profit <i>more</i> by selling the option.		NotationsStock pricecCall pricexExercise pricerRisk-free rate of returnτTime to expiration	
For example, consider the 40-April option. One could exercise it to get the profit $42\frac{7}{8} - 40 = 2\frac{7}{8}$ . However it would be better just to sell the option, for $3\frac{3}{8}$ . The <i>intrinsic value</i> of an option is its value if the expiration were immediate: the greater of zero and what one would make by exercising the option now. The claim is that the market value of an option always <i>exceeds</i> the intrinsic value. 13			
Financial Economics	Arbitrage and Option Pricing	Financial Economics	Arbitrage and Option Pricing
No Ear	y Exercise		
If one exercises the call at the	present time, one has $s - x$ .		
If one sells the stock short now and covers by exercising the call at expiration, the present value is		Dividend	
$r = re^{-r\tau}$		This argument assumes that the stock pays no dividend.	
The call must be worth at least this much, so		If there is a dividend, it may pay to exercise early, to capture the dividend.	
$c \ge s - x \mathrm{e}^{-r\tau} > s - x.$			
Consequently it does not pay	to exercise before expiration.		
15		16	
Financial Economics	Arbitrage and Option Pricing		
Intuition			
To exercise an option of course precludes future exercise. The possibility of future exercise has some value, and to exercise an			

possibility of future exercise has some value, and to exercise a option before expiration forfeits this value. Consequently one should not exercise an option before expiration.