

Name: .....

1] Please complete the following sentences:

A] A subset  $H$  of a group  $G$  is a *subgroup* if and only if the following two conditions hold:

- for every  $h, k \in H$  .....
- for every  $h \in H$  .....

B] A subgroup  $H$  of a group  $G$  is *normal* if and only if for every  $a \in G$  and for every  $h \in H$  .....

.....

C] A function  $f: G \rightarrow G'$  from a group  $G$  to a group  $G'$  is a *homomorphism* if and only if for every  $a, b \in G$

.....

D] The *kernel* of a homomorphism  $f: G \rightarrow G'$  is  $\ker(f) = \{ \dots \}$ .

2] Are the following statements true or false? Please circle your answers.

A] For every homomorphism  $f: G \rightarrow G'$  we have  $e \in \ker(f)$  ..... TRUE | FALSE

B] For every homomorphism  $f: G \rightarrow G'$ ,  $\ker(f)$  is a normal subgroup of  $G$  ..... TRUE | FALSE

C] A homomorphism  $f: G \rightarrow G'$  is injective if and only if  $\ker(f) = \{e\}$  ..... TRUE | FALSE

D] A homomorphism  $f: G \rightarrow G'$  is surjective if and only if  $\ker(f) \neq \{e\}$  ..... TRUE | FALSE

E] I would like my third lowest quiz grade to be dropped, too ..... TRUE | FALSE